Touch Input on Curved Surfaces
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ABSTRACT
Advances in sensing technology are currently bringing touch input to non-planar surfaces, ranging from spherical touch screens to prototypes the size and shape of a ping-pong ball. To help interface designers create usable interfaces on such devices, we determine how touch surface curvature affects targeting. We present a user study in which participants acquired targets on surfaces of different curvature and at locations of different slope. We find that surface convexity increases pointing accuracy, and in particular reduces the offset between the input point perceived by users and the input point sensed by the device. Concave surfaces, in contrast, are subject to larger error offsets. This is likely caused by how concave surfaces hug the user’s finger, thus resulting in a larger contact area. The effect of slope on targeting, in contrast, is unexpected at first sight. Some targets located downhill from the user’s perspective are subject to error offsets in the opposite direction from all others. This appears to be caused by participants acquiring these targets using a different finger posture that lets them monitor the position of their fingers more effectively.

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General terms: Human factors.

INTRODUCTION
Recent advances in sensor technology have allowed touch-enabling non-planar surfaces. Examples include capacitive sensors in Rekimoto’s Smart Skin [17] and in Apple’s Magic Mouse, resistive sensors in the UnMousePad [18], and FTIR-based sensing in Mouse 2.0 [24]. We also have started to see non-planar touch screens, such as Sphere [3]. For large touch surfaces, such as Sphere, surface curvature is comparably small. The smaller the device, however, the stronger the average curvature becomes, as illustrated by Figure 2. The surface of the DI-based Mouse 2.0 corresponds to a Ø15cm sphere and by sensing touch through an optical fiber bundle, FlyEye [29] manages to touch-enable a Ø 4cm ping-pong ball. As sensing technology continues to evolve, it seems plausible that even smaller devices, such as watches or even electronic jewelry, might become touch sensitive in the near future, resulting in touch surfaces of extreme curvature.

As researchers and engineers create these future touch devices, the question arises of how to design usable interfaces for them. Unfortunately, there is no empirical data about the human factors of touch on curved surfaces yet.

On flat surfaces, touch is comparably well understood. In particular, there is a series of studies investigating the factors responsible for the inaccuracy of touch, including the fat finger problem [26] and the (generalized) perceived input point model [26, 13]. While this paper is only a first step, our ultimate goal is to create similar metric for the usability of object surfaces of arbitrary shape and curvature. Such a metric would allow industrial designers to assess the usability of devices, similar to how the measurement of wind resistance has brought rigor to the design of the shape of cars.

Touch on arbitrary shapes is of very high dimensionality, because device, hands, and the way they can make contact are all of very high degree of freedom. As a first step, we select a tractable, self-contained subset of variables, namely, single touch on spherical shapes, as these already fit existing devices.

We present a user study in which participants acquired targets on surfaces of different curvature and at locations of different slope. We report how surface curvature affects pointing accuracy (preview in Figure 1). We provide minimum button sizes to help interface designers find the best
location for their controls on a curved surface. We also report systematic error offsets that allow engineers to increase the accuracy of their devices by compensating for them [13].

RELATED WORK
The work presented in this paper is related to non-planar touch-sensitive objects and to research on touch input.

Non-planar touch devices
Curved touch devices include relative pointing devices, such as the aforementioned Mouse 2.0 [24], and absolute pointing devices/touch screens, such as Sphere [3]. Devices can be touch-enabled using a range of technologies, such as capacitive (e.g., Smart skin [17]), resistive UnMousePad [18], and optical (e.g., FTIR [9, 24]). Many other sensor concepts could be adapted to non-planar surfaces, such as GelForce, a device that extracts directional pressure from touch [25].

Figure 2: Selection of curved touch devices by decreasing curvature: (a) Microsoft Sphere, (b) FTIR-based and (c) DI-based Mouse 2.0, and (d) FlyEye (not to scale).

In addition to the rigid devices mentioned earlier, curved surfaces also occur as a side effect of deformable devices, including Organic User Interfaces, such as Paper Windows [12]. Objects may either be deformed by users, such as the optically sensed PhotoelasticTouch [19], Gummi [20], or even human skin (Skinput [11]), or objects may be deformed using a device, such as inflatable buttons [10].

While the majority of non-planar devices are still input-only, we are starting to see the first non-planar or deformable touch screens, to date primarily using projection [2].

Touch and angles between finger and surface
Several researchers have found systematic effects that cause a touch device to sense touch at an offset from the intended target. The Shift technique includes a corrective offset that compensates for differences between target location and the perceived input point [26]. Benko et al. noticed that the center of the contact area moves under pressure [2]. Forlines et al. found that touching a target using a flat finger angle leads to an offset input location [7]. Wang and Ren found that finger posture and motion impact the size of the contact area [27]. Holz and Baudisch found that differences in finger roll as well as differences in users' mental models result in additional offsets. They generalized the concept of offsets into the generalized perceived input point model [13]. Follow-up work by the same authors [14] explains error offsets as a conceptual mismatch between users and devices: users target by placing a fixed point located on top of their fingernail over the target. Touch devices, in contrast, determine the contact point as the center of the contact area between finger and device.

Measuring touch targeting error as offset + spread
Because of the presence of systematic offsets, researchers have started to specify touch inaccuracy using two variables, i.e., offset and spread [13] (also referred to as constant and variable error [5]). Since we use this metric to report our results, we discuss it in additional detail.

Each targeting interaction produces a contact point, generally computed as the center of gravity of all points in the contact area, e.g., the center of an oval fitted to the contact area (Figure 3a). All contact points together can now be summarized using two variables:

Error offset refers to the distance between the centroid of a cluster of contact points and the target, measured in millimeters (Figure 3c). Offsets can be compensated for by applying corrective offsets, which is a method for increasing the accuracy of a touch device. Offsets are therefore particularly relevant for device designers.

Figure 3: We report targeting error as offset + spread. (a) A series of trials results in contact points. (b) Contact points are aggregated into a centroid. (c) Offset is defined as the distance between the centroid and the target; spread is the size of the smallest button to contain 95% of all contact points.

Error spread is the remaining error after error offsets have been compensated for (Figure 3c). Spread is measured as a
minimum button size, i.e., the diameter of the smallest circular button in millimeters that still contains 95% of all target acquisitions [13]. Note that this assumed button is centered on the centroid, not the target.

The findings in this paper allow us to extend this reasoning about offset and spread to curved surfaces.

GENERALIZING FROM FLAT TO CURVED SURFACES
In this section, we attempt to generalize what we know about touch on flat surfaces to curved surfaces. We use this to derive the hypotheses for our user study.

On flat surfaces, a finger of given posture always makes contact with the surface the same way. When we generalize to curved surfaces, the curvature of the surface affects the shape and size of the contact area. As illustrated by Figure 4, convex surfaces curve away from the finger, resulting in a smaller contact area. Concave surfaces, in contrast, hug the finger, which leads to a larger contact area.

![Figure 4: The contact area between finger and device (a) increases for concave and (b) decreased for convex surfaces.](image)

In addition, the individual patches of a curved surface have different slopes, which causes the finger to make contact with the surface at different angles.

Our initial hypothesis was that users would maintain a constant finger posture, as shown in Figure 5a. For downhill slopes (from the user’s perspective) this would have caused their fingers to form a flatter angle with the surface, yielding a larger contact area between finger and surface, and thus would have potentially caused larger offsets.

![Figure 5: (a) Our initial hypothesis was that users would acquire all targets with the same finger posture. (b) Piloting, however, revealed that most participants target downhill slopes using a hooked finger.](image)

During piloting, however, we found that the finger contact area was largely unchanged across downhill and uphill facing slopes. Closer inspection revealed that our assumption about the finger posture was wrong. Instead, participants had targeted on downhill slopes with a hooked finger, as illustrated by Figure 5b. This posture allowed participants to hit the target surface at a roughly constant angle, which helped them minimize the contact area between their finger and the touch surface.

Hypotheses
Given that larger contact areas correlated with larger offsets on flat surfaces [13], we hypothesized that the same holds for curved surfaces. Because of the finger hugging property of concave surfaces we hypothesize

H1: Concavity increases offsets, convexity reduces it
For the same reasons we hypothesized

H2. Concavity increases spread, convexity reduces it
The observed variations in finger postures prevented us from formulating a clear hypothesis on surface slope—since flat surfaces offer nothing to reach around, hooked finger postures had not been studied here. Which posture would lead to better targeting was hard to predict. Consequently, rather than formulating a hypothesis we decided to

Q1: Explore effect of uphill/downhill slope on offset
Q2: Explore effect of uphill/downhill slope on spread

CURVE TOUCH: STUDY PROTOTYPE BASED ON FTIR
To be able to analyze the impact of the factors discussed above, we needed a device that could observe the exact contact area between the finger and the touch surface in high resolution. Since diffuse illumination (e.g., [10]) delivers only vague contour data, and capacitive sensing (such as Smart Skin [17]) is hard to manufacture for high and non-interpolated resolution, we opted for a custom design based on FTIR [9], technology previously used, for example, in Mouse 2.0 [24]. FTIR offers high resolution, a comparably crisp contact area outline, as well as reliable recognition of contact. On the flipside, FTIR starts bleeding out light with increasing curvature, which required us to make a series of modifications.

![Figure 6: The FTIR-based touch device we built to sense touch on curved surfaces (curve touch).](image)
Creating exact curvatures by stamping
To obtain exact surface curvatures, we deformed the acryl-
ic using a series of stamps, as illustrated by Figure 7. We
heated the acrylic locally using a heat gun (Figure 7a).
Once malleable, we stamped shapes of the desired curva-
ture into the acrylic (Figure 7b). Resting the acrylic on a
larger ring allowed us to create the hemispherical target
surface as well as a smoother transition to its periphery,
which helped reduce light leakage (see next section). We
obtained best results using 3mm acrylic sheets, which are
thin enough to allow for easy deformation, yet still thick
enough to allow for the injection of light.

Figure 7: We created curved touch surfaces by (a) heating up
the acrylic touch surface using a heat gun and (b) stamping
curved objects (e.g. a silver sphere) into it.

Figure 8 shows six of the stamps we have experimented
with. The four sizes we used in our user studies are hig-
highlighted in bold face.

Figure 8: The stamps we used to make curved surfaces.

Design modifications for the curved touch surface
The necessity of distinguishing the light resulting from
touch from other light sources required us to make some
modifications:

1. No compliant surface: FTIR is most commonly used with
a compliant surface layer to increase the frustration of light
on contact. Unfortunately, the strong curvature of some of
the shapes we used made it difficult to obtain accurately
fitting compliant surfaces. We consequently dropped the
compliant surface from our design. Instead, we used sili-
cone spray to increase frustration when necessary.

2. Light leakage: Light leakage is inherent to all waveguides
and only depends on curvature. It was not an issue at the
actual bulge because the remaining light was strong enough
and because we eliminated brightness differences by thre-
sholding. At the edge of the bulge, it manifested as hot-
pots in the camera image (Figure 9b), because light was
reflected off the opposite side of the bulge and into the
camera as illustrated by Figure 9a. Smoothing the transition
between bulge and periphery reduced the problem far
enough that we could suppress it using thresholding.

Figure 9: (a) Light injected from behind this bulge leaks at the
transition from flat surface to bulge. (b) The same scene as
seen by the built-in camera. The light injected from the right
is reflected off the bulge and shows up as a hotspot on the left.

Exchangeable touch surfaces
To support multiple curvatures, we created different top
units, each of which consisted of a differently deformed
acrylic sheet with illumination (Figure 10). Snap connec-
tors made from Lego bricks assured precise positioning of
the top unit yet allowed replacing top units quickly. We
also added a flat top unit to obtain a total of nine surfaces: a
flat unit plus four curved units that could be flipped to
serve as convex or concave shapes.

Figure 10: We implement different curvatures by using repla-
ceable top units.

Compensating for optical distortion
The small fixed-focus lens offers a high depth of field, thus
a clear image for all shapes. However, perspective effects
make the curvature of the touch surfaces appear distorted.
In particular, surface patches on convex bulges appear
larger, because they are located further away from the cam-
era; in addition, tilted surface patches appear deformed,
because of foreshortening. A universally applicable correc-
tion for this distortion would require switching to a 3D
representation of the surface.

Since we were only concerned with the relative position of
contact points with respect to the target, however, we
treated the respective patch of surface as if it were flat,
which allowed us to scale with a simple linear transforma-
tion. We first restored the apparent size of the respective
patch by scaling it proportional to its distance to the camera
lens. We then stretched points by scaling them with the
corresponding patch ratio.
USER STUDY: IMPACT OF CURVATURE ON ACCURACY

In this study, we investigated the impact of target curvature on touch accuracy. Participants acquired targets on the\textit{curve touch}. Using different top units, we varied \textit{curvature} in nine levels from convex to flat to concave. By using multiple targets placed across the curved surface we also varied \textit{slope}. Our goal was to test the hypotheses discussed earlier, i.e., to determine how curvature and slope impact offsets and spread.

We took the following three measures to minimize the impact of other potential factors. First, participants kept their heads in a fixed position above the touchpad, as shown in Figure 11, which controlled for parallax. Second, the use of a footswitch allowed us to avoid artifacts common with other commit methods, such as inadvertent motion during take-off. The unified button and target acquisition using the footswitch helped reduce participants’ cognitive load. Finally, participants were told to focus on accuracy not on speed; consequently, we did not record task completion time.

**Independent Variables: Curvature and Slope**

Curvatures were implemented using the five top units (see in Figure 10). We varied slope by using targets at different locations on the curved surface. 8 targets were organized in a ring located at 45° zenith angle for each curved surface; in addition there was a single target at the apex.

To prevent participants from (unintentionally) biasing their targeting towards open space we added a second ring of unused/fake crosses further outside. In addition, participants were told that there was no penalty for getting close to other targets during targeting. Note that there was no reason to include real distracter targets though. Distracters have a major effect on \textit{adaptive} input techniques, such as magnetic targets (e.g., [1]), but not on unmodified touch.

**Experimental design**

The study used a 9 × 9 within-participant design, with independent variables curvature (convex or concave Ø13mm, Ø19mm, Ø32mm and flat) and slopes (i.e. 8 targets in a ring at 45° zenith plus apex). Participants performed 6 trials for each curvature.

Curvature was counterbalanced within participants using a partial Latin Square design. The order of targets was randomized. Each participant completed all conditions: 9 curvatures × 9 target orientations × 6 trials = 486 trials per participant.

Participants performed 5 minutes of training before the experiment. They were allowed to take breaks every 54 selections. They completed the study in 45 minutes or less.

**Participants**

We recruited 12 right-handed participants (2 female) from our institution. They were between 20 and 32 years old. They received a small compensation for their time, and we awarded €20 to the most accurate participant.
Hypotheses
Our goal was to investigate our 4 hypotheses and questions:
H1: Concavity increases offsets, convexity reduces it
H2: Concavity increases spread, convexity reduces it
Q1: Explore effect of uphill/downhill slope on offset
Q2: Explore effect of uphill downhill slope on spread

In addition, we wanted to verify that this basic observation for flat surfaces continues to hold true on curved surfaces:
H0: Offsets are oriented along the user's finger

Results
Figure 13 shows the resulting raw data, i.e., all contact points by all participants as recorded during the study.

![Figure 13: Raw data: all touch locations of all participants by curvature and target orientation/target.](image)

H0: Offsets are oriented along the user's finger
All contact points of all targets combined showed an offset of 1.9mm. Its direction matched the direction of participant’s fingers closely, i.e., it was off by only 5.1° clockwise from the 45° participant finger angle. This suggests that offsets are most likely the result of finger direction, rather than, say, head position, which should have produced a north/south oriented offset. This observation matches finger direction offsets previously observed on flat surfaces [13] and supports our hypothesis H0.

The overall effect shows reasonably clearly in Figure 13, where most contact point clusters are offset to the bottom right with respect to their target. An exception is the concave Ø49mm shape. Unlike any of the other curvatures, it showed virtually no global offset, but target-specific offsets towards the center. We discuss this effect in more detail below, and investigated it in a brief follow-up study, also presented in this paper.

H1: Concavity increases offsets, convexity reduces it
A one way ANOVA found a main effect of curvature on offset ($F_{8,88}=5.24, p<.0001$). Post-hoc comparison tests (using a Tukey’s HSD test) indicated the significant differences shown in Figure 14a.

![Figure 14: (a) Error offset by surface curvature (+/- 95% confidence, * significantly different) (b) Linear regression.](image)

The x-axis is curvature measured as 1/radius.

To understand this relationship better we performed linear regressions (Figure 14b). A single linear regression explains a significant portion of offset ($r^2=.7768, F_{1,7}=24.36, p<.001$) for the length of the projection vector: $L = -.45 \times$ curvature+ 3.1. Performing regression separately for convex and concave obtains a better fit: for convex ($r^2=.9187, F_{1,2}=22.61, p<.04, L = -.76 \times \text{curvature} + 3.5$) and for concave ($r^2=.9752, F_{1,2}=78.77, p<.01, L = - \text{curvature} + 2.53$).

These results support our hypothesis H1, i.e., error offsets indeed decreased with convexity and increased with concavity, as suggested by their differences in contact area (Figure 4). These findings integrate nicely with the related work on flat surfaces [13], while generalizing from flat to curved surfaces.

H2: Concavity increases spread, convexity reduces it
Figure 15 illustrates spread across curvatures. Note that we computed spread on a per-user basis. Intuitively, this means that each bar indicates how closely the contact points of a single user are collocated for a target on the respective curvature. For a device to exploit this it needs to employ a per-user calibration, as suggested by [13].

A two way ANOVA found a main effect of curvature on spread ($F_{8,88}=7.62, p<.0001$). Post-hoc multiple means comparison tests found the significant differences shown in Figure 15.
The left half of Figure 15, i.e., the one depicting accuracy on convex shapes, is in general support of our hypothesis H2: spread indeed decreased with increasing convexity. The concave shapes, in contrast, came out unexpectedly. Rather than spread increasing further with concavity, spread eventually even decreased.

Figure 16 suggests one possible explanation for this effect. First, a tight cavity confines the finger, which provides users with tactile feedback that can help adjust the position of their finger. Second, the stronger the curvature, the shorter the part of the bowl that is actually concave. The space around the bowl has to be convex in order to connect the concave bowl to the rest of the surface. For very strong curvatures, users’ fingers fill out the concave part, so that variations in finger posture lead to changes in the contact area on the convex part, where it leads to smaller changes in contact area, thus reduced spread.

This effect is inherent to the nature of curved surfaces: unlike flat surfaces, curved surfaces are finite and the stronger the curvature, the smaller the surface. This holds for concave, as well as convex, as illustrated also by the FlyEye shown in Figure 2.

Q1: Effect of uphill/downhill slope on offset
As illustrated by Figure 19, participants acquired different targets using different finger postures. For targets located on downhill slopes, participants were more likely to employ a hooked finger posture, while they were more likely to use a straight finger to acquire targets located on uphill slopes. When analyzing slope, we grouped target locations that resulted in similar finger postures, as shown in Figure 17.

A two way ANOVA found a main effect of curvature ($F_{2,88}=5.25, p<.0001$), slope ($F_{2,22}=10.60, p<.001$) and the interaction curvature×slope ($F_{16,176}=7.02, p<.0001$) on offset. Figure 18 shows pair wise differences.

Post-hoc multiple means comparison tests (using a Tukey’s HSD test) found that the offsets of downhill slopes were generally smaller than the offsets of center slopes, which in turn were smaller than the offsets of uphill slopes. As apparent also in Figure 18, however, this effect was entirely caused by the concave surfaces.

One possible explanation for the smaller offsets on downhill slopes is differences in finger posture, i.e., that a hooked finger leads to smaller offsets than a straight finger. On flat surfaces, touch inaccuracy has been attributed to users’ inability to monitor the soft fleshy bottom of the finger [26, 14]. As illustrated by Figure 19, users pointing using a hooked finger can see that bottom side. The now invisible side, i.e., the fingernail, is less malleable and thus suffers from the fat finger problem to a much lesser extent.
Q2: Effect of uphill downhill slope on spread
A two-way ANOVA found no significant effects of slope on spread.

Summary
In summary, by adding curvature as a factor, we have generalized the concept of error offsets from flat surfaces [13] to curved surfaces. We found that error offsets depend on curvature (H1) and slope (Q1). Both factors influence error offset, but there is an interaction and most of the error offset of concave targets comes from the uphill slope, where users are forced to target using a straight finger. The effects of curvature on spread, in contrast, are moderate. There appears to be an effect for convex targets. For concave targets in contrast, multiple confounding factors compensate for each other.

FOLLOW-UP STUDY ON CONCAVE
As discussed earlier, we speculated that the smallness of the error offsets of the concave targets was caused by participants targeting using a hooked finger. To verify this assumption, we conducted an informal follow-up study with a small number of additional participants. Participants again repeatedly acquired crosshair targets of different orientations. Our main hypothesis was that the lack of offsets on concave surfaces was an artifact of participants employing different finger postures. To investigate this, we varied finger posture this time.

Interface & Apparatus & Task
We used the same curve touch device, screen, button, and footswitch setup as in the main user study (Figure 11). We limited the study to the Ø49mm concave surface, which had displayed the pattern most clearly. Participants performed the same task as before.

To obtain additional data for the slope variable, we broke the single target ring at 45° zenith angle from the previous study down into an inner ring at 30° and an outer ring at 60° zenith angle for an overall 8 outer + 8 inner + 1 apex = 17 targets.

Additional independent variable: Finger posture
(1) In the fingertip condition, participants were instructed to acquire all targets using their fingertip. This caused them to acquire targets using a straight finger for the uphill targets and to hook their finger for the downhill targets. (2) In the flat finger condition, they acquired all targets as with a flat finger. This forced them to use a straight finger also for downhill targets. (3) In the free condition participants acquired each target as they chose to—which corresponded to the first study. In order not to influence participants in the free condition, we ran the free condition first. We then counterbalanced the following fingertip and flat finger conditions.

Experimental design
The study used a 3x17 within-participant design, with independent variables finger posture (fingertip, flat finger, free) and slope (17 targets organized in two rings plus apex). Participants performed six trials for each finger posture and slope. The order of target orientations was randomized. Each participant completed all conditions, i.e., 3 finger postures x 17 target orientations x 6 trials = 306 trials per participant.

Participants performed 5 minutes of training before the experiment. They were allowed to take breaks every 34 selections. They all completed the study in 30 minutes or less.

Participants
We recruited 6 new right-handed participants (2 female) from our institution. They were between 24 and 30 years old. They again received a small compensation for their time and we awarded €20 to the most accurate participant.

Hypotheses
Our main hypothesis was that the unexpected lack of a finger direction offset of the Ø49mm surface would only happen in the free and fingertip conditions, but that the flat finger condition would still be subject to the offset.

H0: Offsets are oriented along the user’s finger

Results
Figure 20 and Figure 21 show the raw data, i.e., all contact points obtained during the study by fingertip, flat finger, and free conditions.

As in the main study, the overall error offset of the free condition pointed towards the center rather than in the direction of the finger (the component of the error offset across all targets/slopes pointing in the direction of the finger measured only 0.8mm). This held across all targets including the additional ring of outer targets. For the fingertip condition the finger direction offset was equally small (0.9mm). In the flat finger condition, however, we did see a major offset in the direction of the finger (2.4mm).

Figure 20: (a) Contact points in the free condition and (b) how much the free condition resembled the fingertip condition.

We reconstructed participants’ finger posture in the free condition by comparing the contact area sizes for each touch with the fingertip and flat finger conditions. Figure 20b illustrates that participants effectively targeted with the fingertip throughout; a slight tendency towards using a flat finger in the bottom right was weak enough that it had little effect on the error offsets.
Discussion
The results of this informal study indicate that the error offsets in the concave condition of the main study are indeed an artifact of finger posture. By switching between a straight and hooked finger, participants always targeted using the finger tip, thereby targeting more accurately in the sense that offsets were reduced.

What remains is the question why the more strongly curved concave conditions seemed to benefit less from the hooked finger posture (see also Figure 13). Figure 22 attempts to explain this by illustrating an effect we observed during piloting. For strongly concave surfaces, a hooked finger posture introduces additional targeting errors when it accidentally touches the opposite side of the bowl (Figure 22a). Most pilot users avoided the issue by switching back to a straight finger posture. This avoids the accidental touches, at the expense of reintroducing the increased offset error of the straight finger.

IMPLICATIONS FOR DESIGN
On the one hand, the findings presented in this paper are intended to deepen our understanding of targeting on non-planar surfaces. On the other hand, the same findings can be used to inform the design of curved touch devices as well as the design of interfaces running on such devices.

For device designers, we found two additional factors influencing error offsets, namely surface curvature and slope. Knowledge of these offsets allows engineers to compensate for these effects by coding corrective offsets into their device drivers, which will increase device accuracy (as demonstrated for flat surfaces by [13]).

For interface designers, minimum button sizes are relevant, because they help design usable interfaces. Our findings suggest placing targets on points of extreme curvatures in order to make them easier to acquire, so application designers might want to use them for frequently used functions.

CONCLUSIONS
Our findings indicate that the curvature of touch surfaces impacts targeting in terms of spread/minimum button size and in particular in terms of systematic offsets. This information can help designers of curved touch devices improve their devices.

As future work, we plan to study the impact of shape on more complex interactions, such as grasping. New findings in this space may one day provide the missing link between HCI and the disciplines that have discussed form factor and shape all along, such as industrial design.

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